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# Flow-Based Policy for Online Reinforcement Learning

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## Abstract

1 We present **FlowRL**, a novel framework for online reinforcement learning that  
2 integrates flow-based policy representation with Wasserstein-2-regularized opti-  
3 mization. We argue that in addition to training signals, enhancing the expressive-  
4 ness of the policy class is crucial for the performance gains in RL. Flow-based  
5 generative models offer such potential, excelling at capturing complex, multimodal  
6 action distributions. However, their direct application in online RL is challenging  
7 due to a fundamental objective mismatch: standard flow training optimizes for  
8 static data imitation, while RL requires value-based policy optimization through a  
9 dynamic buffer, leading to difficult optimization landscapes. FlowRL first models  
10 policies via a state-dependent velocity field, generating actions through determinis-  
11 tic ODE integration from noise. We derive a constrained policy search objective  
12 that jointly maximizes Q through the flow policy while bounding the Wasserstein-2  
13 distance to a behavior-optimal policy implicitly derived from the replay buffer.  
14 This formulation effectively aligns the flow optimization with the RL objective,  
15 enabling efficient and value-aware policy learning despite the complexity of the pol-  
16 icy class. Empirical evaluations on DMControl and Humanoidbench demonstrate  
17 that FlowRL achieves competitive performance in online reinforcement learning  
18 benchmarks.

## 19 1 Introduction

20 Recent advances in iterative generative models,  
21 particularly Diffusion Models (DM) [16, 37] and  
22 Flow Matching (FM) [22, 23, 40], have demon-  
23 strated remarkable success in capturing complex  
24 multimodal distributions. These models excel in  
25 tasks such as high-resolution image synthesis [7],  
26 robotic imitation learning [6, 2], and protein struc-  
27 ture prediction [17, 3], owing to their expressivity  
28 and ability to model stochasticity. A promising yet  
29 underexplored application lies in leveraging their  
30 multimodal generation capabilities to enhance re-  
31 inforcement learning (RL) policies, particularly  
32 in environments with highly stochastic or multi-  
33 modal dynamics.

34 Traditional RL frameworks alternate between Q-function estimation and policy updates [38], often  
35 parameterizing policies as Gaussian [13] or deterministic policies [36, 12] to maximize expected  
36 returns. However, directly employing diffusion or flow-based models as policies introduces a  
37 fundamental challenge: the misalignment between RL objectives, which aim to optimize value-aware  
38 distributions, and generative modeling, which imitates static data distributions. This discrepancy

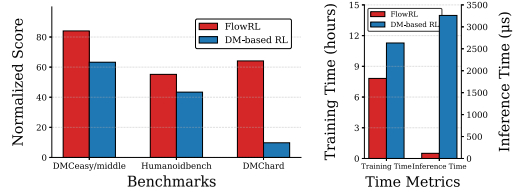


Figure 1: (left) Normalized scores comparing FlowRL and DM-based RL (QVPO) on 12 challenging DMC-hard and HumanoidBench tasks, and 3 DMC-easy & middle tasks. (right) Computational efficiency on the Dogrun task: 1M-step training time and single env step inference time.

39 becomes exacerbated in online RL, where nonstationary data distributions and evolving Q-value  
40 estimates lead to unstable training [12].

41 While recent methods have pioneered the use of diffusion model (DM)-based policies in online  
42 reinforcement learning [44, 8, 42], these approaches still suffer from high computational cost and  
43 inefficient sample usage (see Section 2). By contrast, flow-based models (FMs), despite their ability  
44 to represent complex and multimodal policies, have yet to be effectively integrated into online RL  
45 frameworks.

46 Our method distinguishes itself by leveraging carefully selected replay buffer data as a reference  
47 distribution to align flow-based policies with high-value behaviors while preserving multimodality.  
48 Inspired by prior works such as SIL [27] and OBAC [25], which utilised behaviour policies to  
49 guide policy optimization but limit policy expressivity to capture diverse behaviors, we propose a  
50 unified framework that integrates flow-based action generation with Wasserstein-2-regularized [10]  
51 distribution matching. Specifically, our policy extraction objective simultaneously maximizes Q-  
52 values through flow-based actor and minimizes distribution distance from high-reward trajectories  
53 identified in the replay buffer. By reformulating this dual objective as a guided flow-matching loss, we  
54 enable the policy to adaptively imitate empirically optimal behaviors while exploring novel actions  
55 that maximize future returns. Besides, this approach retains the simplicity of standard actor-critic  
56 architectures, without requiring lengthy iterative sampling steps or auxiliary inference tricks [18,  
57 8]—yet fully exploits the multimodality of flow models to discover diverse, high-performing policies.  
58 We evaluate our approach on challenging DMControl [39] and HumanoidBench [35], demonstrating  
59 competitive performance against state-of-the-art baselines. Notably, our framework achieves one-step  
60 policy inference, significantly reducing computational overhead and training instability caused by  
61 backpropagation through time (BPTT) [42, 30]. Experimental results highlight both the empirical  
62 effectiveness of our method and its practical advantages in scalability and efficiency, establishing a  
63 robust pathway for integrating expressive generative models into online RL.

## 64 2 Related Work

65 In this section, we provide a comprehensive survey of existing policy extraction paradigms based  
66 on iterative generative models based policy, with a particular focus on recent advances that leverage  
67 diffusion and flow-based models in offline or online reinforcement learning. We categorize these  
68 approaches according to their underlying policy optimization objective and highlight their respective  
69 advantages and limitations.

70 **Generalized Behavior Cloning** Generalized Behavior Cloning, often akin to weighted behavioral  
71 cloning or weighted regression [32, 31], trains policies by imitating high-reward trajectories from a  
72 replay buffer, weighted by advantage or value estimates, thereby avoiding BPTT. Previous methods  
73 like EDP [18], QGPO [24], QVPO [8], and QIPO [45] implemented these paradigms, enhancing  
74 computational efficiency by bypassing BPTT. However, as demonstrated in prior research, this  
75 approach has been empirically shown to be inefficient [29, 30], and often leads to suboptimal  
76 performance.

77 **Reverse process as policy parametrizations** These methods use reparameterized policy gradients,  
78 computing gradients of the Q-function with respect to policy parameters directly through the generative  
79 model’s reverse sampling process, similar to the reparameterization trick commonly employed  
80 in Gaussian-based policies [13]. Previous methods, such as DQL [43], DiffCPS [15], Consistency-  
81 AC [9], and DACER [42], backpropagate gradients through the reverse diffusion process, which,  
82 while flexible, incurs significant computational costs due to iterative denoising and backpropagation  
83 through time (BPTT) [29]. These factors limit the scalability of such algorithms to more complex  
84 environments. To address this, FQL [30] distills a one-step policy from a flow-matching policy,  
85 reducing computational cost, but requires careful hyperparameter tuning.

86 **Other Approaches.** Beyond above methods, alternative methods include action gradients [44, 33],  
87 hybrid Markov Decision Processes (MDPs) [34], rejection sampling [4] or combinations of above  
88 strategies [26].

89 The distinction between these methods underscores an inherent trade-off between computational  
90 simplicity and the efficiency of policy extraction. Generalized Behavior Cloning emphasizes ease

of implementation, often at the expense of policy extraction efficiency. In contrast, reparameterized policy gradients facilitate direct policy updates but incur increased complexity. These observations highlight the necessity for further research to achieve a better balance between expressivity and scalability when applying iterative generative models to reinforcement learning.

### 3 Preliminaries

#### 3.1 Reinforcement Learning

Consider the Markov Decision Process (MDPs) [1] defined by a 5-tuple  $\mathcal{M} = \langle \mathcal{S}, \mathcal{A}, \mathcal{P}, r, \gamma \rangle$ , where  $\mathcal{S} \in \mathbb{R}^n$  and  $\mathcal{A} \in \mathbb{R}^m$  represent the continuous state and action spaces,  $\mathcal{P}(s'|s, a) : \mathcal{S} \times \mathcal{A} \rightarrow \Delta(\mathcal{S})$  denotes the dynamics distribution of the MDPs,  $r(s, a) : \mathcal{S} \times \mathcal{A} \rightarrow \Delta(\mathbb{R})$  is a reward function,  $\gamma \in [0, 1)$  gives the discounted factor for future rewards. The goal of RL is to find a policy  $\pi(a|s) : \mathcal{S} \rightarrow \Delta(\mathcal{A})$  that maximizes the cumulative discounted reward:

$$J_\pi = \mathbb{E}_{\pi, \mathcal{P}} \left[ \sum_{t=0}^{\infty} \gamma^t r(s_t, a_t) \right]. \quad (1)$$

In this paper, we focus on the online off-policy RL setting, where the agent interacts with the environment and collects new data into a replay buffer  $\mathcal{D} \leftarrow \mathcal{D} \cup \{(s, a, s', r)\}$ . The replay buffer consequently maintains a distribution over trajectories induced by a mixture of historical behavior policies  $\pi_\beta$ . At the  $k$ -th iteration step, the online learning policy is denoted as  $\pi_k$ , with its corresponding  $Q$  value function defined by:

$$Q^{\pi_k}(s, a) = \mathbb{E}_{\pi_k, \mathcal{P}} \left[ \sum_{t=0}^{\infty} \gamma^t r(s_t, a_t) | s_0 = s, a_0 = a \right], \quad (2)$$

and it can be derived by minimizing the TD error [38]:

$$\arg \min_{Q^{\pi_k}} \mathbb{E}_{(s, a, r, s') \sim \mathcal{D}} \left[ (Q^{\pi_k}(s, a) - \mathcal{T}^{\pi_k} Q^{\pi_k}(s, a))^2 \right], \quad (3)$$

where  $\mathcal{T}^{\pi_k} Q^{\pi_k}(s, a) = r(s, a) + \gamma \mathbb{E}_{s' \sim \mathcal{P}(\cdot|s, a), a' \sim \pi_k(\cdot|s')} [Q^{\pi_k}(s', a')]$ .

Similarly, we distinguish the following key elements:

- **Optimal policy and Q-function:** The optimal policy  $\pi^*$  maximizes the expected cumulative reward, and the associated Q-function  $Q^*(s, a)$  characterizes the highest achievable return.
- **Behavior policy and replay buffer:** The behavior policy  $\pi_\beta$  is responsible for generating the data stored in the replay buffer [21, 25]. Its Q-function,  $Q^{\pi_\beta}(s, a)$ , reflects the expected return when following  $\pi_\beta$ . Notably,  $\mathcal{D}$  is closely tied to the distribution of  $\pi_\beta$ , such that actions sampled from  $\mathcal{D}$  are supported by those sampled from  $\pi_\beta$  (i.e.,  $a \in \mathcal{D} \Rightarrow a \sim \pi_\beta$ ).
- **Behavior-optimal policy:** Among all behavior policies present in the buffer, we define  $\pi_{\beta^*}$  as the one that achieves the highest expected return, with Q-function  $Q^{\pi_{\beta^*}}(s, a)$ .

These definitions yield the following relationship, which holds for any state-action pair:

$$Q^*(s, a) \geq Q^{\pi_{\beta^*}}(s, a) \geq Q^{\pi_\beta}(s, a). \quad (4)$$

This relationship suggests that, although direct access to the optimal policy is typically infeasible, the value of the optimal behavior policy constitutes a theoretical lower bound [27] on the performance that can be achieved by policies derived from the replay buffer.

#### 3.2 Flow Models

Continuous Normalizing Flows (CNF) [5] model the time-varying probability paths by defining a transformation between an initial distribution  $p_0$  and a target data distribution  $p_1$  [22, 23]. This transformation is parameterized by a flow  $\psi_t(x)$  governed by a learned time-dependent vector field  $v_t(x)$  [5], following the ordinary differential equation (ODE):

$$\frac{d}{dt} \psi_t(x) = v_t(\psi_t(x)), \quad (5)$$

and the continuity equation [41]:

$$\frac{d}{dt} p_t(x) + \nabla \cdot [p_t(x) v_t(x)] = 0, \quad \forall x \in \mathbb{R}^d. \quad (6)$$

**Flow Matching.** Flow matching provides a theoretically grounded framework for training continuous-time generative models through deterministic ordinary differential equations (ODEs). Unlike diffusion models that rely on stochastic dynamics governed by stochastic differential equations (SDEs) [37], flow matching operates via a *deterministic* vector field, enabling simpler training objectives and more efficient sampling trajectories. The core objective is to learn a neural velocity field  $v_\theta : [0, 1] \times \mathbb{R}^d \rightarrow \mathbb{R}^d$  that approximates a predefined conditional target velocity field  $u(t, x|x^1)$ . Given a source distribution  $q(x^0)$  and target distribution  $p(x^1)$ , the training process involves minimizing the conditional flow matching objective [22]:

$$\mathcal{L}_{\text{CFM}}(\theta) = \mathbb{E}_{\substack{t \sim \mathcal{U}([0,1]) \\ x^1 \sim p, x^0 \sim q}} \|v_\theta(t, x^t) - u(t, x^t|x^1)\|_2^2, \quad (7)$$

where the linear interpolation path is defined as  $x^t = tx^1 + (1-t)x^0$  with  $u(t, x^t|x^1) = x^1 - x^0$ . This formulation induces a *probability flow* governed by the ODE:

$$\frac{dx}{dt} = v_\theta(t, x), \quad x^0 \sim q, \quad (8)$$

which transports samples from  $q$  to  $p$ .

## 4 Method

In this section, we detail the design of our method. We first parameterize the policy as a flow model, where actions are generated by integrating a learned velocity field over time. For policy improvement, we model policy learning as a constrained policy search that maximizes expected returns while bounding the distance to an optimal behavior policy. Practically, we circumvent intractable distribution matching and optimal behavior policy by aligning velocity fields with elite historical actions through regularization and implicit guidance, enabling efficient constraint enforcement.

### 4.1 Flow Model based Policy Representation.

We parameterize  $\pi_\theta$  with  $v_\theta(t, s, a^t)$ , a state-action-time dependent velocity field, as an actor for reinforcement learning. The policy  $\pi_\theta$  can be derived by solving ODE (8) :

$$\pi_\theta(s, a^0) = a^0 + \int_0^1 v_\theta(t, s, a^t) dt, \quad (9)$$

where  $a^0 \sim \mathcal{N}(0, I^2)$ . The superscript  $t$  denotes the continuous time variable in the flow-based ODE process to distinguish it from discrete Markovian time steps in reinforcement learning. (For brevity, the terminal condition at  $t = 1$  is omitted in the notation.) The Flow Model derives a deterministic velocity field  $v_\theta$  from an ordinary differential equation (ODE). However, when  $a^0$  is sampled from a random distribution, the model effectively functions as a stochastic actor, exhibiting diverse behaviors across sampling instances. This diversity in generated trajectories inherently promotes enhanced exploration in online reinforcement learning.

Recall the definition in Section 3.1. Following the notation of  $\pi_\beta$  and  $\pi_{\beta^*}$ , we can define the corresponding velocity fields as follows:

Let  $v_\beta$  be the velocity field induced by the behavior policy  $\pi_\beta$ , such that:

$$v_\beta(s, a) = a - a^0.$$

where  $s, a \sim \mathcal{D}$ , and  $a^0 \sim \mathcal{N}(0, I^2)$ .

Similarly, let  $v_{\beta^*}$  denote the velocity field induced by the behavior-optimal policy  $\pi_{\beta^*}$ :

$$v_{\beta^*}(s, a) = a - a^0.$$

where  $a \sim \pi_{\beta^*}$ , and  $a^0 \sim \mathcal{N}(0, I^2)$ .

## 4.2 Optimal-Behavior Constrained Policy Search with Flow Models

Building on the discussion in Section 3.1, where the optimal behavior policy is established as a lower bound for the optimal policy, we proceed to optimize the following objective under a constrained policy search setting:

$$\begin{aligned} \theta^* &= \arg \max_{\theta} \mathbb{E}_{a \sim \pi_{\theta}} [Q^{\pi_{\theta}}(s, a)], \\ \text{s.t. } D(\pi_{\theta}, \pi_{\beta^*}) &\leq \epsilon. \end{aligned} \quad (10)$$

Here,  $D(\pi_{\theta}, \pi_{\beta^*})$  denotes a distance metric between the current policy and the optimal behavior policy distributions.

The objective is to maximize the expected reward  $\mathbb{E}_{a \sim \pi_{\theta}} [Q^{\pi_{\theta}}(s, a)]$  while constraining the learned policy  $\pi_{\theta}$  to remain within an  $\epsilon$ -neighborhood of the optimal behavior policy  $\pi_{\beta^*}$ , i.e.,  $D(\pi_{\theta}, \pi_{\beta^*}) \leq \epsilon$ . This formulation utilizes the Q-function, a widely used and effective approach for policy extraction, while ensuring fidelity to the optimal behavior policy. Despite its theoretical appeal, this optimization paradigm exhibits two inherent limitations:

- *Challenges in computing distributional distances:* For flow-based models, computing policy densities at arbitrary samples is computationally expensive, which limits the practicality of distance metrics such as the KL divergence for sample-based estimation and policy regularization.
- *Inaccessibility of the optimal behavior policy  $\pi_{\beta^*}$ :* The replay buffer contains trajectories from a mixture of policies, making it difficult to directly sample from  $\pi_{\beta^*}$  or to reliably estimate its associated velocity field, thereby complicating the computation of related quantities in practice.

## 4.3 A Tractable Surrogate Objective

To overcome the aforementioned challenges, we propose the following solutions:

- **Wasserstein Distance as Policy Constraints:** We introduce a policy regularization method based on the alignment of velocity fields. This approach bounds the Wasserstein distance between policies by characterizing their induced dynamic transport processes, thereby imposing direct empirical constraints on the evolution of policies without requiring density estimation.
- **Implicit Guidance for Optimal Behaviors:** Instead of explicitly constraining the policy to match the inaccessible  $\pi_{\beta^*}$ , we leverage implicit guidance from past best-performing behaviors in the buffer, enabling efficient revisiting of arbitrary samples and encouraging the policy to remain within a high-quality region of the action space.

In particular, we adopt the squared Wasserstein-2 distance for its convexity with respect to the policy distribution and ease of implementation. This metric is also well-suited for measuring the velocity field between policies and enables efficient sample-based regularization within the flow-based modeling framework. In general, we can define the Wasserstein-2 Distance [41] as follows :

**Definition 4.1 (Wasserstein-2 Distance)** Given two probability measures  $p$  and  $q$  on  $\mathbb{R}^n$ , the squared Wasserstein-2 distance between  $p$  and  $q$  is defined as:

$$W_2^2(p, q) = \inf_{\gamma \in \Pi(p, q)} \int_{\mathbb{R}^n \times \mathbb{R}^n} \gamma(x, y) \|x - y\|^2 dx dy, \quad (11)$$

where  $\Pi(p, q)$  denotes the joint distributions of  $p$  and  $q$ ,  $\gamma$  on  $\mathbb{R}^n \times \mathbb{R}^n$  with marginals  $p$  and  $q$ . Specifically, we derive a tractable upper bound for the Wasserstein-2 distance (proof in A.1):

**Theorem 4.1 (W-2 Bound for Flow Matching)** Let  $v_{\theta}$  and  $v_{\beta^*}$  be two velocity fields inducing time-evolving distributions  $\pi_{\theta}^t(a|s)$  and  $\pi_{\beta^*}^t(a|s)$ , respectively. Assume  $v_{\beta^*}$  is Lipschitz continuous in  $a$  with constant  $L$ .  $a^t = ta + (1 - t)a^0$ . Then, the squared Wasserstein-2 distance between  $\pi_{\theta}$  and  $\pi_{\beta^*}$  at  $t = 1$  satisfies:

$$W_2^2(\pi_{\theta}, \pi_{\beta^*}) \leq e^{2L} \int_0^1 \mathbb{E}_{a \sim \pi_{\beta^*}} [\|v_{\theta}(s, a^t, t) - v_{\beta^*}\|^2] dt. \quad (12)$$

By explicitly constraining the Wasserstein-2 distance, the model enforces proximity between the current policy and the optimal policy stored in the buffer. This objective is inherently consistent

with the generative modeling goal of minimizing distributional divergence. The regularization mechanism benefits from the representational expressiveness of flow-based models in capturing diverse, high-performing action distributions while systematically restricting policy updates.

However, while the upper bound of Wasserstein-2 distance above is theoretically tractable, sampling directly from  $\pi_{\beta^*}$  or evaluating its velocity field remains a computational barrier in practice. To circumvent this limitation, we introduce an implicit guidance (13) mechanism through the  $Q^{\pi_{\beta^*}}$ , which is more readily estimable:

$$\mathbb{E}_{a' \sim \pi_{\theta}, t \sim \mathcal{U}(0,1)} \left[ f(Q^{\pi_{\beta^*}}(s, a) - Q^{\pi_{\theta}}(s, a')) \|v_{\theta}(s, a^t, t) - (a - a^0)\|^2 \right], \quad (13)$$

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$$f \propto \max(Q^{\pi_{\beta^*}} - Q^{\pi_{\theta}}, 0). \quad (14)$$

The constraint incorporates a non-negative weighting function, as defined in Eq. (14), thereby establishing an adaptive regularization mechanism. A positive value of  $f$  signifies that the behavioral policy achieves superior performance relative to the current policy; under these circumstances, the constraint adaptively regularizes the current policy towards the optimal behavioral policy.

The implicit form of the constraints in Eq. (12) enables efficient utilization of arbitrary samples from the replay buffer, thus improving sample efficiency. Moreover, by relaxing the strict constraint on the Wasserstein-2 distance, the modified objective enhances computational efficiency. Notwithstanding this relaxation, policy improvement guarantees remain valid, as demonstrated in the following theorem (proof in Appendix A.2):

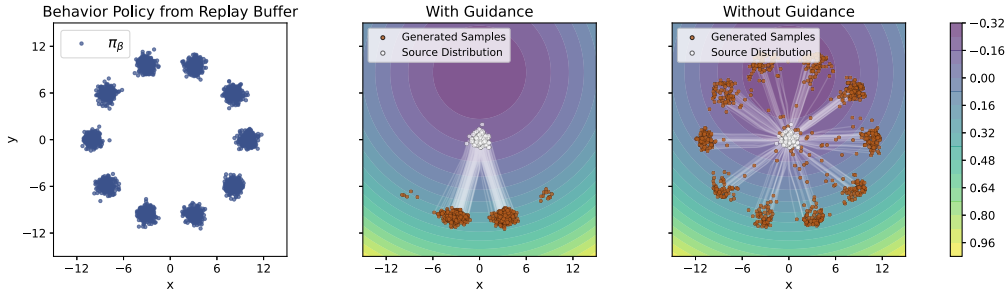


Figure 2: Illustration of Theorem 4.2 on a bandit toy example: (left) behavior data in the replay buffer; (middle) implicit value-guided flow matching steers the policy toward the high-performance behavior policy ( $\pi_{\beta^*}$ ), heatmap shows  $Q^{\pi_k} - Q^{\pi_{\beta^*}}$ , white lines indicate transport paths; (right) standard flow matching leads to dispersed sampling with high variance under limited flow steps.

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**Theorem 4.2 (Weighted CFM)** Let  $\pi_k(a|s)$  be the current policy induced by velocity field  $v_{\theta_k}$ , and  $f$ , a non-negative weighting function with  $f \propto Q^{\pi_{\beta^*}} - Q^{\pi_k}$ . Minimizing the objective (13) yields an improved policy distribution:

$$\pi_{k+1}(a|s) = \frac{f(s, a)\pi_{\beta^*}(a|s)}{\mathcal{Z}(s)}, \quad (15)$$

where  $\mathcal{Z}(s) = \int_{\mathcal{A}} f \cdot \pi_k(a|s) da$  is the normalization factor.

Figure 2 shows that, as guaranteed by Theorem 4.2, flow matching with guidance can steer the policy toward the  $\pi_{\beta^*}$ , even without direct sampling from it. For details of the toy example settings, see Appendix B.4.

#### 224 4.4 A Practical Implementation

Building on the theoretical developments above, we now present a practical implementation of FlowRL, as detailed in Algorithm 1.

227 **Policy Evaluation** Recall the constraint in Eq. (13), which necessitates the evaluation of both the  
 228 current policy value function  $Q^{\pi_\theta}$  and the optimal behavioral policy value function  $Q^{\pi_{\beta^*}}$ . The value  
 229 function  $Q^{\pi_\theta}$  is estimated using standard Bellman residual minimization, as described in Eq. (3). For  
 230  $Q^{\pi_{\beta^*}}$ , leveraging the definition of  $\pi_{\beta^*}$ , we similarly adopt the following objective:

$$\arg \min_{Q^{\pi_{\beta^*}}} \mathbb{E}_{(s,a,r,s') \sim \mathcal{D}} \left[ (Q^{\pi_{\beta^*}}(s,a) - \mathcal{T}^{\pi_{\beta^*}} Q^{\pi_{\beta^*}}(s,a))^2 \right], \quad (16)$$

$$\mathcal{T}^{\pi_{\beta^*}} Q^{\pi_{\beta^*}}(s,a) = r(s,a) + \gamma \mathbb{E}_{s' \sim \mathcal{D}} \left[ \max_{a' \sim \mathcal{D}} Q^{\pi_{\beta^*}}(s',a') \right]. \quad (17)$$

231 To circumvent the difficulties of directly evaluating the max operator, we leverage techniques from  
 232 offline reinforcement learning to estimate  $Q^{\pi_{\beta^*}}$ . Among these approaches, we adopt expectile  
 233 regression [19] due to its simplicity and compatibility with unmodified data pipelines. Specifically,  
 234 the value function  $V^{\pi_{\beta^*}}$  and the action-value function  $Q^{\pi_{\beta^*}}$  are estimated by solving the following  
 235 optimization problems:

$$\arg \min_{V^{\pi_{\beta^*}}} \mathbb{E}_{(s,a) \sim \mathcal{D}} [L_2^\tau(Q^{\pi_{\beta^*}}(s,a) - V^{\pi_{\beta^*}}(s))], \quad (18)$$

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$$\arg \min_{Q^{\pi_{\beta^*}}} \mathbb{E}_{(s,a,s',r) \sim \mathcal{D}} \left[ (r + \gamma V^{\pi_{\beta^*}}(s') - Q^{\pi_{\beta^*}}(s,a))^2 \right], \quad (19)$$

237 where  $L_2^\tau(x) = |\tau - \mathbb{1}(x < 0)|x^2$  denotes the expectile regression loss and  $\tau$  is the expectile factor.

238 **Policy Extraction** Accordingly, the policy extraction problem for flow-based models can be  
 239 formulated as the following constrained optimization:

$$\theta^* = \arg \max_{\theta} \mathbb{E}_{s \sim \mathcal{D}, a \sim \pi_\theta} [Q^{\pi_\theta}(s,a)], \quad (20)$$

240

$$\text{s.t. } \mathbb{E}_{s,a \sim \mathcal{D}, a' \sim \pi_\theta} \left[ f(Q^{\pi_{\beta^*}} - Q^{\pi_\theta}) \|v_\theta(s, a^t, t) - (a - a^0)\|^2 \right] \leq \epsilon. \quad (21)$$

241 Although a closed-form solution can be derived using the Lagrangian multiplier and KKT conditions,  
 242 it is generally intractable to apply in practice due to the unknown partition function [31, 32, 25].  
 243 Therefore, we adopt a Lagrangian form, leading to the following objective:

$$\mathcal{L}(\theta) = \mathbb{E}_{s,a \sim \mathcal{D}, a' \sim \pi_\theta} \underbrace{[Q^{\pi_\theta}(s,a')]}_{\text{exploration}} - \lambda \left( \underbrace{f(Q^{\pi_{\beta^*}} - Q^{\pi_\theta}) \|v_\theta(s, a^t, t) - (a - a^0)\|^2}_{\text{exploitation}} - \epsilon \right). \quad (22)$$

244 Where  $\lambda$  is the Lagrangian multiplier, which is often set as a constant in practice [11, 20].

245 Objective (22) can be interpreted as comprising two key components: (1) maximization of the  
 246 learned Q-function, which encourages the agent to explore unknown regions and facilitates policy  
 247 improvement; and (2) a policy distribution regularization term, which enforces alignment with optimal  
 248 behavior policies and thereby promotes the exploitation of high-quality actions.

249 Conceptual similarities exist between our method and both self-imitation learning [27] and tandem  
 250 learning [28]. Self-imitation learning focuses on exploiting high-reward behaviors by encouraging  
 251 the policy to revisit successful past experiences, typically requiring complete trajectories and modifica-  
 252 tions to the data pipeline. In contrast, our method operates directly on individual samples from  
 253 the buffer, enabling more flexible and efficient sample utilization. Tandem learning, by comparison,  
 254 decomposes the learning process into active and passive agents to facilitate knowledge transfer, with  
 255 a primary emphasis on value learning, whereas our approach is centered on policy extraction.

## 256 5 Experiments

257 To comprehensively evaluate the effectiveness and generality of **FlowRL**, we conduct experiments  
 258 on a diverse set of challenging tasks from DMControl [39] and HumanoidBench [35]. These  
 259 benchmarks encompass high-dimensional locomotion and human-like robot (Unitree H1) control  
 260 tasks. Our evaluation aims to answer the following key questions:

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**Algorithm 1** Flow RL
 

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**Require:** Critic  $Q^{\pi_\theta}$ , critic  $Q^{\pi_{\beta^*}}$ , value  $V^{\pi_{\beta^*}}$ , flow model  $v_\theta$ , replay buffer  $\mathcal{D} = \emptyset$ , weighting function  $f$

```

1: repeat
2:   for each environment step do
3:      $a \sim \pi_\theta(a|s), \quad r, s' \sim P(s'|s, a)$ 
4:      $\mathcal{D} \leftarrow \mathcal{D} \cup \{(s, a, s', r)\}$ 
5:   end for
6:   for each gradient step do
7:     Estimate value for  $\pi_\theta$  : Update  $Q^{\pi_\theta}$  by (3),
8:     Estimate value for  $\pi_{\beta^*}$  : Update  $Q^{\pi_{\beta^*}}$  by (19), update  $V^{\pi_{\beta^*}}$  by (18)
9:     Update  $v_\theta$  by (22)
10:  end for
11: until reach the max environment steps
  
```

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- 261 1. How does FlowRL compare to previous online RL algorithms and existing diffusion-based online  
 262 algorithms?
- 263 2. Can the algorithm still demonstrate strong performance in the absence of any explicit exploration  
 264 mechanism?
- 265 3. How does the constraint affect the performance?

266 We compare **FlowRL** against two categories of baselines to ensure comprehensive evaluation: **(1)**  
 267 **Model-free RL:** We consider three representative policy parameterizations: deterministic policies  
 268 (TD3 [12]), Gaussian policies (SAC [13]), and diffusion-based policies (QVPO [8], the previous  
 269 state-of-the-art for diffusion-based online RL). **(2) Model-based RL:** TD-MPC2 [14], a strong model-  
 270 based method on these benchmarks, is included for reference only, as it is not directly comparable to  
 271 model-free methods.

## 272 5.1 Results and Analysis

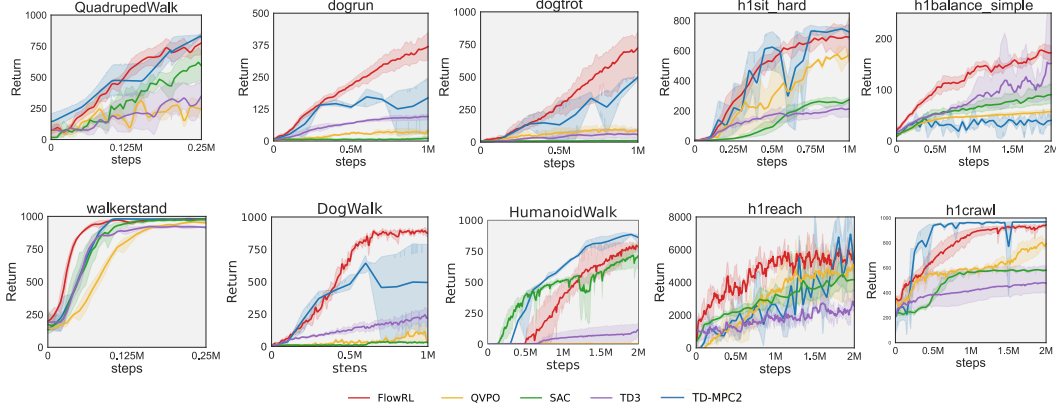
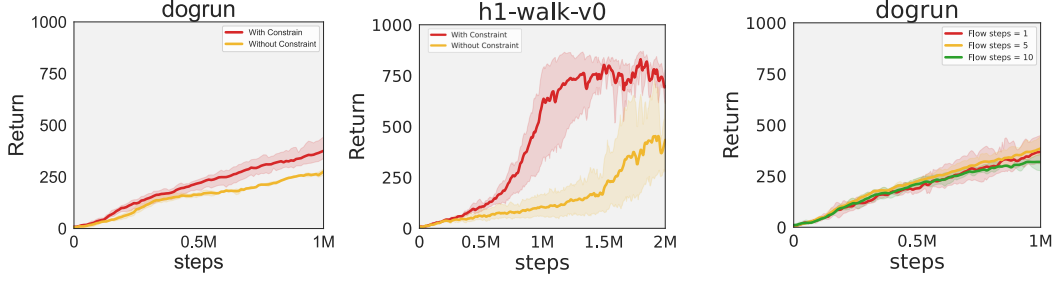


Figure 3: Main results. We provide performance comparisons for tasks (first column: DMC-easy/middle; second and third columns: DMC-hard; fourth and fifth columns: HumanoidBench). For comprehensive results, please refer to Appendix D. All model-free algorithms (FlowRL, SAC, QVPO, TD3) are evaluated with 5 random seeds, while the model-based algorithm (TD-MPC2) uses 3 seeds. Note that direct comparison between model-free methods and the model-based TD-MPC2 is not strictly fair; TD-MPC2 is included just as a reference.

273 The main results are summarized in Figure 3, which shows the learning curves across tasks. **FlowRL**  
 274 consistently outperforms or matches the model-free baselines on the majority of tasks, demonstrating  
 275 strong generalization and robustness, especially in challenging high-dimensional (e.g., the DMC dog  
 276 domain, where  $s \in \mathbb{R}^{223}$  and  $a \in \mathbb{R}^{38}$ ) and complex control settings (e.g., Unitree H1). Compared



(a) Effect of the constraint: FlowRL with the constraint achieves higher returns compared to the variant without the constraint.

(b) Sensitivity to flow steps: The number of flow steps has a limited effect on FlowRL performance.

Figure 4: Ablation studies

to strong model-based baselines, FlowRL achieves comparable results but is much more efficient in terms of wall-clock time. Notably, both during the training and evaluation stage, we use flow steps  $N = 1$ , and do not employ any sampling-based action selection used in [8, 18]. Despite the absence of any explicit exploration mechanism, FlowRL demonstrates strong results, which can be attributed to both the inherent stochasticity and exploratory capacity of the flow-based actor and the effective exploitation of advantageous actions identified by the policy constraint. These findings indicate that, while exploration facilitates the discovery of high-reward actions, the exploitation of previously identified advantageous behaviors is equally essential.

## 5.2 Ablation Studies

One of the central designs in FlowRL is the introduction of a policy constraint mechanism. This design aims to guide the policy towards optimal behavior by adaptively weighting the constraint based on the relative advantage of the optimal behavioral policy over the current policy. To rigorously assess the necessity and effectiveness of this component, we address **Q3** by conducting ablation studies in which the policy constraint is omitted from FlowRL. Experimental results in Figure 4a indicate that the presence of the policy constraint leads to improvements in performance and, by constraining the current policy towards the optimal behavioral policy, enhances sample efficiency. These benefits are especially pronounced in environments with complex dynamics (e.g., H1 control tasks from HumanoidBench), highlighting the importance of adaptive policy regularization in challenging task settings.

We also investigate the sensitivity of the algorithm to different choices of the number of flow steps ( $N=1,5,10$ ). Experimental results in Figure 4b demonstrate that varying the number of flow steps has only a limited impact on the overall performance. Specifically, using a smaller number of flow steps does not substantially affect the final policy performance. On the other hand, increasing the number of flow steps results in longer backpropagation through time (BPTT) chains, which significantly increases computational complexity and training time. These findings suggest that FlowRL is robust to the choice of flow step and that single-step inference is generally sufficient for achieving stable and efficient learning in practice.

## 6 Conclusion

We introduce FlowRL, a practical framework that integrates flow-based generative models into online reinforcement learning through Wasserstein-2 distance constrained policy search. By parameterizing policies as state-dependent velocity fields, FlowRL leverages the expressivity of flow models to model action distributions. To align policy updates with value maximization, we propose an implicit guidance mechanism that regularizes the learned policy using high-performing actions from the replay buffer. This approach avoids explicit density estimation and reduces iterative sampling steps, achieving stable training and improved sample efficiency. Empirical results demonstrate that FlowRL achieves competitive performance.

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## A Proofs in the Main Text

Here, we present a sketch of theoretical analyses in Figure 5. We model the policy learning as a constrained policy search that maximizes expected returns while bounding the distance to an optimal behavior policy. To avoid sampling from  $\pi_\beta^*$ , we employ guided flow matching, which allows the constraint to utilize arbitrary data from the buffer. Finally, we solve the problem using Lagrangian relaxation.

### A.1 Proof for Theorem 4.1

Before the proof, we first introduce the following lemma [10]:

**Lemma 1** : Let  $\psi_1^t(x_0)$  and  $\psi_2^t(x_0)$  be the two different flow maps induced by  $v_1^t$  and  $v_2^t$  starting from  $x^0$ , and assume  $v_2^t$  are Lipschitz continuous in  $x$  with constant  $L$ . Define their difference as  $\Delta_t(x^0) = \psi_1^t(x^0) - \psi_2^t(x^1)$ . (For notational consistency, we denote the time variable as a superscript.) Then the difference satisfies the following inequality:

$$\frac{d}{dt} \Delta_t(x_0) \leq ||v_1^t(\psi_1^t(x^0)) - v_2^t(\psi_1^t(x^0))|| + L||\Delta_t(x_0)||$$

By rewriting equivalently, we have:

$$\frac{d}{dt} \Delta_t(x^0) = \underbrace{v_1^t(\psi_1^t(x^0)) - v_2^t(\psi_1^t(x^0))}_{\delta_v(t)} + \underbrace{v_2^t(\psi_1^t(x^1)) - v_2^t(\psi_2^t(x^0))}_{\delta_\psi(t)}$$

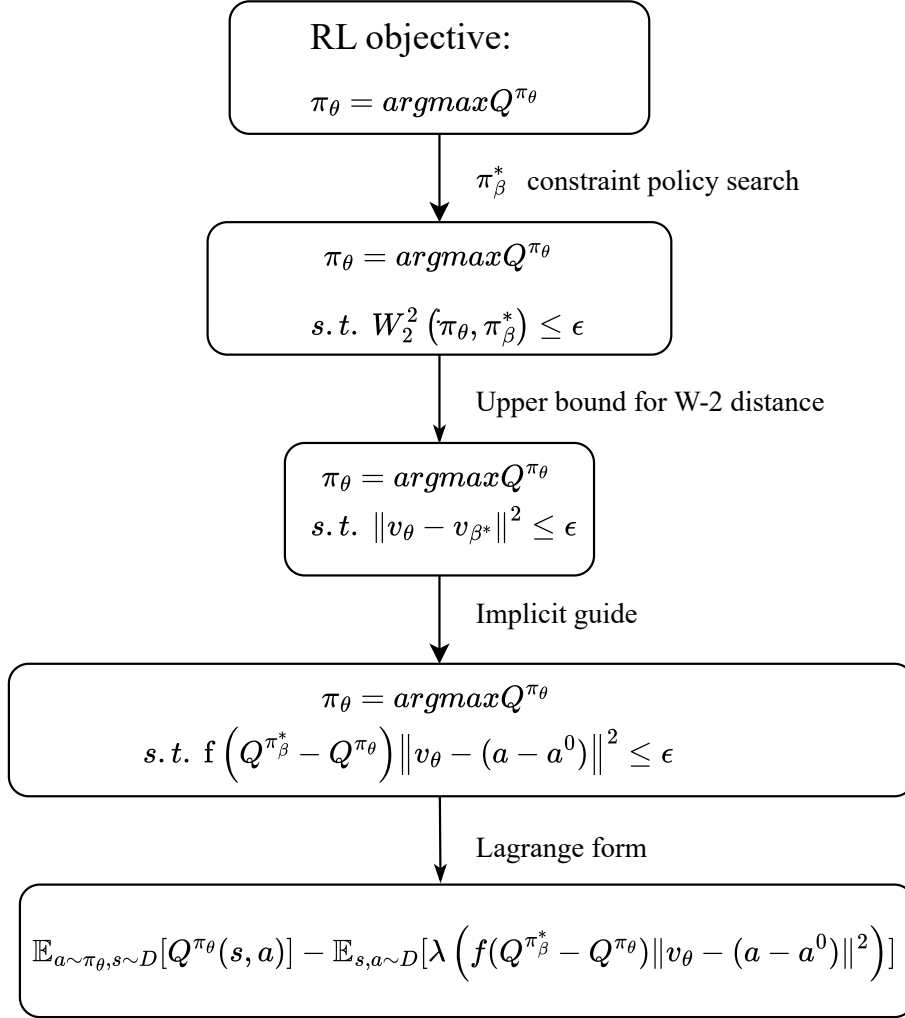


Figure 5: Theoretical sketch of FlowRL

441 Since  $v_2^t$  is Lipschitz continuous in  $x$  with constant  $L$ , we have:

$$\|v_2^t(x) - v_2^t(y)\| \leq L\|x - y\|$$

442 By Lipschitz continuity,

$$\|\delta_\psi(t)\| \leq L\|\Delta_t(x^0)\|$$

443 Then,

$$\left\| \frac{d}{dt} \Delta_t(x^0) \right\| \leq \|\delta_v(t)\| + L\|\Delta_t(x^0)\|$$

444 This concludes the proof of the inequality satisfied by the difference of the two flow maps.

445 Let  $v_\theta$  and  $v_{\beta^*}$  be two velocity fields that induce time-evolving distributions  $\pi_\theta^t(a|s)$  and  $\pi_{\beta^*}^t(a|s)$ ,  
 446 respectively((we omit the superscript  $t = 1$  for policy distributions, i.e.,  $\pi_\theta(a|s) := \pi_\theta^1(a|s)$ )).  
 447 Assume  $v_{\beta^*}$  is Lipschitz continuous with constant  $L$ . Then, define  $f(t) = \|\Delta_t(x_0)\|$ , by Lemma  
 448 1, we have:

$$\frac{d}{dt} f(t) \leq \|\delta_v(t)\| + Lf(t),$$

449 where  $\delta_v(t) = v_\theta(t, \psi_t^\theta(s, a^0)) - v_{\beta^*}$ . Then, we have,

$$\frac{d}{dt} (e^{-Lt} f(t)) \leq e^{-Lt} \|\delta_v(t)\|.$$

450 Then we can get (by simply intergrating from 0 to t both side and multiplying  $e^{-Lt}$ ):

$$e^{-Lt} f(t) - f(0) \leq \int_0^t e^{-Lm} \|\delta_v(m)\| dm.$$

451 The initial policy distribution  $a^0 \sim p(a^0)$  is shared between the two velocity fields, so  $f(0) = 0$ .

452 Therefore,

$$f(t) \leq e^{Lt} \int_0^t e^{-Lm} \|\delta_v(m)\| dm.$$

453 At  $t = 1$ ,

$$f(1) \leq e^L \int_0^1 e^{-Lm} \|v_\theta(s, \psi_\theta^t(s, a^0), m) - v_{\beta^*}\| dm.$$

454 By taking the expectation and using Jensen's inequality:

$$\mathbb{E}_{a^0}[f(1)^2] \leq e^{2L} \int_0^1 \mathbb{E}_{a \sim \pi_\theta^t} [\|v_\theta(s, a, t) - v_{\beta^*}\|^2] dt.$$

455 And use the definition of the Wasserstein-2 distance:

$$W_2^2(\pi_\theta, \pi_{\beta^*}) = \inf_{\gamma \in \Pi(\pi_\theta, \pi_{\beta^*})} \int_{\mathbb{R}^n \times \mathbb{R}^n} \|x - y\|^2 d\gamma(x, y),$$

456 where  $\Pi(\pi_\theta, \pi_{\beta^*})$  denotes the set of all couplings between  $\pi_\theta$  and  $\pi_{\beta^*}$ . Construct the following  
457 coupling  $\gamma$  and define:

- 458 •  $a_\theta^1 = \psi_\theta^1(x_0)$ ,
- 459 •  $a_{\beta^*}^1 = \psi_{\beta^*}^1(x_0)$ .

460 By definition, the coupling  $\gamma$  is defined via the joint distribution of  $(a \sim \pi_\theta, a \sim \pi_{\beta^*})$  induced by  
461  $a_0 \sim p_0$ . So, for any coupling  $\gamma$ ,

$$W_2^2(\pi_\theta, \pi_{\beta^*}) \leq \int_{\mathbb{R}^n \times \mathbb{R}^n} \|x - y\|^2 d\gamma(x, y).$$

462 With the constructed coupling substituted, we have

$$\int_{\mathbb{R}^n \times \mathbb{R}^n} \|x - y\|^2 d\gamma(x, y) = \mathbb{E}_{a^0} [\|\psi_\theta^1(a^0) - \psi_{\beta^*}^1(a^0)\|^2] = \mathbb{E}_{a^0}[f(1)^2].$$

463 Recall that the flow-based policy models transport the initial distribution  $p_0(a^0)$  to the final policy  
464 distributions  $\pi_\theta$  and  $\pi_{\beta^*}$  at  $t = 1$ . The squared Wasserstein-2 distance between  $\pi_\theta$  and  $\pi_{\beta^*}$  can be  
465 bounded as

$$W_2^2(\pi_\theta, \pi_{\beta^*}) \leq \mathbb{E}_{a^0}[f(1)^2]. \quad (23)$$

466 Thus,

$$W_2^2(\pi_\theta, \pi_{\beta^*}) \leq e^{2L} \int_0^1 \mathbb{E}_{a \sim \pi_\theta^t} [\|v_\theta(s, a^t) - v_{\beta^*}(s, a)\|^2] ds. \quad (24)$$

## 467 A.2 Proof for Theorem 4.2

468 The weighted loss can be written as:

$$\mathcal{L}_W(\theta) = \int_{s \sim D} \rho(s) \int_{s, a \sim D} f(s, a) \pi_k(a|s) \|v_\theta(s, a^t, t) - (a - a^0)\| da ds$$

469 where  $\rho(s)$  is the state distribution in replay buffer,  $a^0 \sim \mathcal{N}(0, I^2)$ ,  $t \sim \mathcal{U}(0, 1)$ ,  $a^t = ta + (1-t)a^0$ .

470 Assuming the weighted policy distribution is:

$$\pi_{k+1}(a'|s) = \frac{f(s, a) \pi_k(a|s)}{\mathcal{Z}(s)}, \quad \text{where} \quad \mathcal{Z}(s) = \int_{s, a \sim D} f(s, a) \pi_k(a|s) da.$$

471 Substituting above  $\pi_{k+1}(a'|s)$  into the loss function, we have:

$$\mathcal{L}_W(\theta) = \int_{s \sim D} \rho(s) \mathcal{Z}(s) \int_{s, a \sim D} \pi_{k+1}(a'|s) \|v_\theta(s, a^t, t) - (a - a^0)\| da ds.$$

472 The expectation form:

$$\mathcal{L}_W(\theta) = \mathbb{E}_{s \sim D, a \sim \pi_{k+1}(a|s)} [\mathcal{Z}(s) \|v_\theta(s, a^t, t) - (a - a^0)\|].$$

473 The gradient of  $\mathcal{L}_W(\theta)$  is:

$$\nabla_\theta \mathcal{L}_W(\theta) = \mathbb{E}_{s \sim D, a \sim \pi_{k+1}(a|s)} [\mathcal{Z}(s) \nabla_\theta \|v_\theta(s, a, t) - (a - a^0)\|].$$

474  $\mathcal{Z}(s)$  does not depend on  $\theta$ , that means, minimizing  $\mathcal{L}_W(\theta)$  is equivalent to minimizing the expected  
475 loss under the new distribution  $\pi_{k+1}(a|s)$ , provided that our assumption holds.

## 476 B Hyperparameters and Experiment Settings

477 In this section, we provide comprehensive details regarding the implementation of FlowRL, the  
478 baseline algorithms, and the experimental environments. All experiments are conducted on a single  
479 NVIDIA H100 GPU and an Intel(R) Platinum 8480C CPU, with two tasks running in parallel on the  
480 GPU.

### 481 B.1 Hyperparameters

482 The hyperparameters used in our experiments are summarized in Table 1. For the choice of the  
483 weighting function, we use  $f(x) = \mathbb{I}(x) \cdot \exp(x)$ , where  $\mathbb{I}(x)$  is the indicator function, i.e.,

$$\mathbb{I}(x) = \begin{cases} 1, & \text{if } x > 0 \\ 0, & \text{otherwise} \end{cases}$$

484 For numerical stability, the  $Q$  function is normalized by subtracting its mean exclusively during the  
485 computation of the weighting function.

### 486 B.2 Baselines

487 In our experiments, we have implemented SAC, TD3, QVPO and TD-MPC2 using their original  
488 code bases and slightly tuned them to match our evaluation protocol to ensure a fair and consistent  
489 comparison.

490 • For SAC [13], we utilized the open-source PyTorch implementation, available at <https://github.com/pranz24/pytorch-soft-actor-critic>.

492 • TD3 [12] was integrated into our experiments through its official codebase, accessible at <https://github.com/sfujim/TD3>.

494 • QVPO [8] was integrated into our experiments through its official codebase, accessible at <https://github.com/wadx2019/qvpo>.

496 • TD-MPC2 [14] was employed with its official implementation from <https://github.com/nicklashansen/tdmpc2> and used their official results.

### 498 B.3 Environment Details

499 We validate our algorithm on the DMControl [39] and HumanoidBench [35], including the most  
500 challenging high-dimensional and Unitree H1 humanoid robot control tasks. On DMControl, tasks  
501 are categorized into DMC easy & middle (walker and quadruped domains), and DMC hard (dog and  
502 humanoid domains). On HumanoidBench, we focus on tasks that do not require dexterous hands.

Table 1: Hyperparameters

	Hyperparameter	Value
<b>Hyperparameters</b>	Optimizer	Adam
	Critic learning rate	$3 \times 10^{-4}$
	Actor learning rate	$3 \times 10^{-4}$
	Discount factor	0.99
	Batchsize	256
	Replay buffer size	$1 \times 10^6$
	Expectile factor $\tau$	0.9
	Lagrangian multiplier $\lambda$	0.1
	Flow steps $N$	1
	ODE Solver	Midpoint Euler
<b>Value network</b>	Network hidden dim	512
	Network hidden layers	3
	Network activation function	mish
<b>Policy network</b>	Network hidden dim	512
	Network hidden layers	2
	Network activation function	elu



Figure 6: Task domain visualizations

#### 503 B.4 Toy Example Setup

504 We consider a 2D toy example as follows. The behavior policy is a Gaussian mixture model with 10  
505 components, each with mean

$$\mu_k = (10 \cos(2\pi k/10), 10 \sin(2\pi k/10)), \quad k = 0, 1, \dots, 9,$$

506 and covariance  $I$ . The initial distribution is a Gaussian  $\mathcal{N}((0, 0), I)$ .  $Q^{\pi_{\beta^*}} - Q^{\pi_{\theta}}$  is defined as

$$\frac{1}{600} \|x - (0, 8.66)\|^2 - 3,$$

507 and  $f(x) = \mathbb{I}(x) \cdot x$ . Flow steps  $N = 5$ .

#### 508 C Limitation and Future Work

509 In this work, we propose a flow-based reinforcement learning framework that leverages the behavior-  
510 optimal policy as a constraint. Although competitive performance is achieved even without explicit  
511 exploration, investigating efficient adaptive exploration mechanisms remains a promising direction  
512 for future research.

Task	State dim	Action dim
Walker Run	24	6
Walker Stand	24	6
Quadruped Walk	78	12
Humanoid Run	67	24
Humanoid Walk	67	24
Dog Run	223	38
Dog Trot	223	38
Dog Stand	223	38
Dog Walk	223	38

Table 2: Task dimensions for DMControl.

Task	Observation dim	Action dim
H1 Balance Hard	77	19
H1 Balance Simple	64	19
H1 Crawl	51	19
H1 Maze	51	19
H1 Reach	57	19
H1 Sit Hard	64	19

Table 3: Task dimensions for HumanoidBench.

## 513 D More Experimental Results

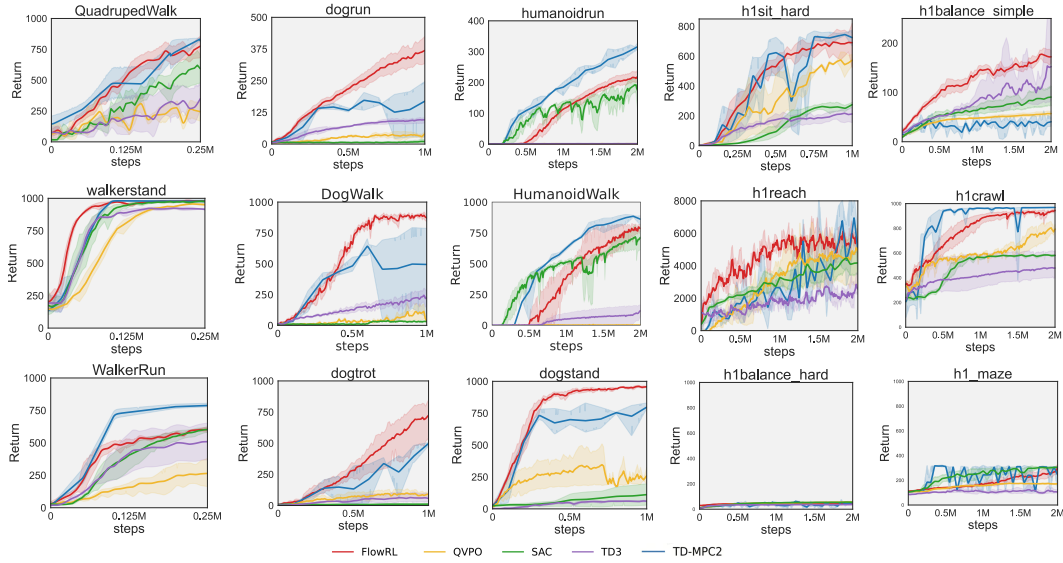


Figure 7: Experimental results are reported on 12 tasks drawn from HumanoidBench and DMC-hard, 3 tasks from DMC-easy & middle.

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